# Deep Manifold Embedding for 3D Object Pose Estimation

Hiroshi Ninomiya[1], Yasutomo Kawanishi[1], Daisuke Deguchi[2], Ichiro Ide[1], Hiroshi Murase[1],
Norimasa Kobori[3] and Yusuke Nakano[3]

[1]*Graduate School of Information Science, Nagoya University, Furo-cho, Chikusa-ku, Nagoya-shi, Aichi, Japan*
[2]*Information Strategy Office, Nagoya University, Furo-cho, Chikusa-ku, Nagoya-shi, Aichi, Japan*
[3]*Toyota Motor Corporation, Toyota-cho, Toyota-shi, Aichi, Japan*
*ninomiyah@murase.m.is.nagoya-u.ac.jp, kawanishi@is.nagoya-u.ac.jp, ddeguchi@nagoya-u.jp,*
*{ide, murase}@is.nagoya-u.ac.jp, {norimasa_kobori, yusuke_nakano}@mail.toyota.co.jp*

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Abstract:     Recently, 3D object pose estimation is being focused. The Parametric Eigenspace method is known as one of the fundamental methods for this. It represents the appearance change of an object caused by pose change with a manifold embedded in a low-dimensional subspace. It obtains features by Principal Component Analysis (PCA), which maximizes the appearance variation. However, there is a problem that it cannot handle a pose change with slight appearance change since there is not always a correlation between pose change and appearance change. In this paper, we propose a method that introduces "Deep Manifold Embedding" which maximizes the pose variation directly. We construct a manifold from features extracted from Deep Convolutional Neural Networks (DCNNs) trained with pose information. Pose estimation with the proposed method achieved the best accuracy in experiments using a public dataset.

## 1 INTRODUCTION

The demand for automated robots for industrial and life-related fields is increasing. In the industrial field, picking up some industrial parts, such as automotive parts and appliance parts, has been automated by robots. Recently, a competition named Amazon Picking Challenge (Correll et al., 2016) was held to improve the technology for picking up 3D objects. Meanwhile, in the life-related field, Human Support Robot, which helps daily life, has been developed for the aging society (Broekens et al., 2009). It will be used for housework, nursing care, and so on. In such situations, the task of picking up 3D objects and handing them over to humans occur frequently. In either cases, it is a common issue for robots to grab an object, so such technology is required. To grab an object, 3D object pose estimation is necessary.

A conventional object pose estimation method (Chin and Dyer, 1986) is based on template matching. This method estimates an object pose by many templates taken from various view points of the target object beforehand. The estimation result is obtained from the best matched template. Thus, many templates are required for accurate pose estimation.



Appearance change: Large
Pose change: 90 deg.

0 deg.    90 deg.

Appearance change: Small
Pose change: 90 deg.
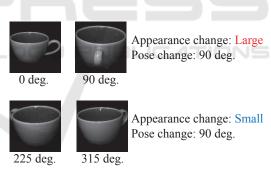
225 deg.    315 deg.

Figure 1: Appearance change and pose change.

To solve this problem, Murase and Nayar proposed the Parametric Eigenspace method (Murase and Nayar, 1995). It represents the pose change of an object with a manifold embedded in a low-dimensional subspace obtained by Principal Component Analysis (PCA). This method can reduce the number of templates since it interpolates unknown poses by cubic spline.

Since PCA focuses only on the appearance of an object, some poses may be mapped to similar points in a low-dimensional subspace in case their appearances differ only slightly, as shown in Figure 1. This deteriorates the pose estimation accuracy. As shown in Figure 2, it is difficult to distinguish between points

Figure 2: Manifold construction by PCA.

mapped to similar points on the manifold in the low-dimensional subspace in case each point corresponds to a very different pose, because PCA is an unsupervised learning method which maximizes the appearance variation; the pose variation is not considered.

This means that it may be difficult to estimate the exact pose of the target object by its overall appearance. Therefore, PCA will not be effective when partial appearance is very important for distinguishing object poses. This gives us the idea of pose estimation by learning the relationship between partial appearance and its exact pose.

In this paper, we propose a supervised feature extraction method for pose manifold considering pose variation. To extract features considering pose variation, we use a supervised learning method instead of an unsupervised learning method such as PCA. We focused on Deep Convolutional Neural Networks (DCNNs) (Krizhevsky et al., 2012), which is one of the deep learning models, as a supervised learning method.

Figure 3 shows the overview of the proposed method. DCNNs demonstrate very high performance on various benchmarks, such as generic object recognition and scene recognition (Razavian et al., 2014), since they can automatically obtain appropriate features for various tasks. For this reason, we considered that pose discriminative features can be obtained by DCNNs trained with pose information as supervisory signals. Therefore we introduce the concept of "Deep Manifold Embedding" that is a supervised feature extraction method for a pose manifold using deep learning technique.

The rest of this paper describes the manifold-based pose estimation method in Section 2, explains the detailed process flow of the proposed method in Section 3, reports evaluation results in Section 4, and concludes the paper in Section 5.

## 2 MANIFOLD-BASED POSE ESTIMATION

Figure 4 shows the process flow of the proposed manifold-based pose estimation method. First, a manifold which represents object pose changes from fea-
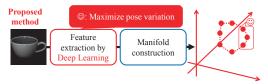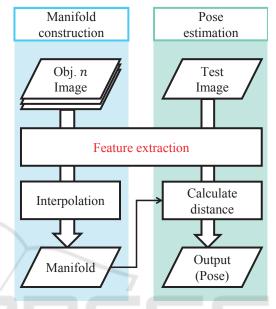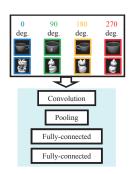


Figure 3: Manifold construction by deep learning.



Figure 4: Process flow of manifold-based pose estimation.

tures obtained by a feature extraction method is constructed. In the pose estimation phase, an input image is projected onto the obtained feature space. Finally, the pose estimation result is obtained from the nearest manifold point.

In order to construct a feature that could distinguish poses, we focused on deep learning as a supervised learning method. Deep learning is a machine learning method, which can learn feature extraction and classification simultaneously. The feature obtained by this method is known to have a higher discriminative power than hand-crafted features (Donahue et al., 2013). For this reason, we should be able to obtain a very effective feature for pose estimation by deep learning trained with pose information. Accordingly, the manifold constructed from the feature obtained by deep learning should be able to handle pose changes even with a slight appearance change, which is difficult to be handled by features obtained by PCA.

We call this supervised feature extraction method for pose manifold using deep learning technique as "Deep Manifold Embedding".
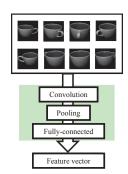
Figure 5: Training DC-NNs with pose information.


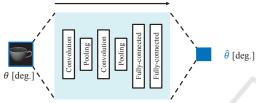
Figure 6: Extracting features from trained DC-NNs.



Figure 8: Pose-CyclicR-Net.



Figure 9: Pose-C-Net.



Figure 7: Pose-R-Net.

# 3 DEEP MANIFOLD EMBEDDING

To obtain the features for manifold construction by deep learning, we first train a DCNN with pose information. Training samples are images with objects taken at arbitrary pose angles around an axis. Figure 5 shows the overview of the training of the DCNN with pose information. In this way, we can train a DCNN which maximizes the pose variation, and thus can obtain very effective features for pose estimation. Then, we extract features from the trained DCNN. Meanwhile, Figure 6 shows the overview of extracting features from the trained DCNN. We input training samples for extracting features to the trained DCNN, and the activations of the middle layer are used as features. Manifolds are constructed from those features with interpolation as same as the conventional Parametric Eigenspace method.

There are various ways of representing pose information. Here, we propose three models with different ways of pose representation;

- Pose-R-Net: Regression model trained with pose information represented by angle (deg.) directly.

- Pose-CyclicR-Net: Regression model trained with pose information represented by trigonometric functions to consider pose cyclicity.

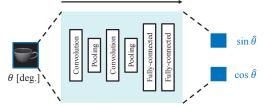- Pose-C-Net: Classification model trained with
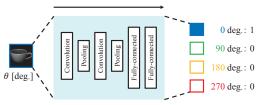
pose information represented as a categorical variable, which means that pose is discretized.

Details of each model are described in the following sections.

## 3.1 Pose-R-Net

Figure 7 shows the overview of the Pose-R-Net. We trained DCNNs with pose information θ represented by degree directly. The number of output layer unit is one. We used squared error as the loss function.

There is a risk that the training loss becomes unfairly big because this model does not consider the cyclictiy of poses. For example, if a 0 deg. sample is estimated as 355 deg., the DCNN trains 355 deg. loss in spite of the fact that the actual loss is only 5 deg.

## 3.2 Pose-CyclicR-Net

Figure 8 shows the overview of the Pose-CyclicR-Net. As same as the Pose-R-Net, this model is a regression model that uses squared error as the loss function. However, here we represent pose information θ as $\sin\theta$ and $\cos\theta$ to consider the cyclicty of poses. Therefore, the number of output layer units is two.

This model is trained with pose information considering pose cyclicity, so it can solve the problem of Pose-R-Net.

## 3.3 Pose-C-Net

Unlike the previous two models, this model solves the pose estimation problem as a pose classification problem.

Figure 10: Object examples in COIL-20 (Nene et al., 1996).



0 deg.　5 deg.　10 deg.
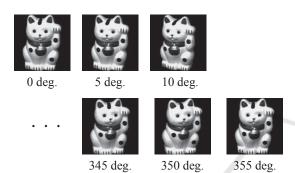
. . .

345 deg.　350 deg.　355 deg.

Figure 11: Examples of pose changes.

Figure 9 shows the overview of the Pose-C-Net. We trained a DCNN with pose information θ as a categorical variable. Therefore, the number of output layer units is the same as the number of pose classes. We used cross entropy as the loss function.

# 4 EVALUATION EXPERIMENTS

To confirm the effectiveness of the proposed method, we conducted pose estimation experiments using a public dataset. We introduce below the dataset and the experimental conditions, and then report and discuss the results from the experiment.

## 4.1 Datasets

We used the public dataset named Columbia Object Image Library (COIL-20) (Nene et al., 1996). It is composed of gray-scale images of 20 objects. Images of the objects were taken at pose intervals of 5 deg. around a vertical axis, and each image size was normalized to $128 \times 128$ pixels. In total, it contains 1,440 images. Figure 10 shows examples of objects in the dataset, and Figure 11 shows the pose change of an object.

Table 1: DCNN architecture.

| Input | Units: $128 \times 128$ |
|---|---|
| Convolution 1 | Kernel: $5 \times 5$<br>Channel: 16<br>Maxpooling: $5 \times 5$ |
| Convolution 2 | Kernel: $5 \times 5$<br>Channel: 32<br>Maxpooling: $5 \times 5$ |
| Fully-connect 3 | Units: 512 |
| Fully-connect 4 | Units: 512 |
| Fully-connect 5 | Units: 512 |
| Output | Units:　1 (Pose-R-Net)<br>Units:　2 (Pose-CyclicR-Net)<br>Units: 36 (Pose-C-Net) |

## 4.2 Experimental Condition

### 4.2.1 DCNN Training

Table 1 shows the network architecture of each DCNN model. The number of output layer units differ for each model because of difference of pose representation, but the other structure is the same. Kernels, weights, and biases were initialized with random values. We used Rectified Linear Units (ReLU) (Nair and Hinton, 2010) as an activation function. Squared loss function was used to train the Pose-R-Net and the Pose-CyclicR-Net models, and cross entropy loss function was used to train the Pose-C-Net. Kernels, weights, and biases were updated by using back-propagation. We used the dropout technique (Hinton et al., 2012) for enhancing the generalization capability. The evaluation was performed in a two-fold cross validation setting. Validation sets were as follows:

- Set 1: 0, 10, 20, $\cdots$, 350 deg.

- Set 2: 5, 15, 25, $\cdots$, 355 deg.

### 4.2.2 Manifold Construction

We evaluated two conventional features and five deep learning based features. The conventional features were (1) a pixel feature, and (2) a PCA feature. Here, the pixel feature is composed of raw pixel values, and the PCA feature is the coefficients obtained from the pixel feature calculated by PCA. Deep learning based features are features extracted from the Pose-R-Net, the Pose-CyclicR-Net, and the Pose-C-Net. In addition, two features extracted from DCNNs trained for object category classification were prepared for comparison. One model trained with object category information including COIL-20 was named Obj-C-Net.

Table 2: Experimental results (Manifold based).

| Manifold | MAE [deg.] |
|---|---|
| Pixel | 1.16 |
| PCA | 1.39 |
| Obj-C-Net | 1.70 |
| OverFeat | 1.89 |
| Pose-R-Net (Proposed) | 1.59 |
| Pose-CyclicR-Net (Proposed) | 1.72 |
| Pose-C-Net (Proposed) | 1.09 |

Table 3: Experimental results (DCNN only).

| DCNN model | MAE [deg.] |
|---|---|
| Pose-R-Net | 28.32 |
| Pose-CyclicR-Net | 9.29 |
| Pose-C-Net | 7.92 |



Figure 12: Experimental results (an object which has very similar appearance poses).

Its structure is the same as the Pose-R-Net, the Pose-CyclicR-Net, and the Pose-C-Net except for the number of output layer units. Obj-C-Net has 20 units in the output layer since COIL-20 is composed of 20 objects. The other model is a pre-trained model with the ImageNet 2012 training set (Deng et al., 2009), named OverFeat (Sermanet et al., 2013). We extracted features from the first fully-connected layer following convolution layers in each DCNN. In other words, the Pose-R-Net, the Pose-CyclicR-Net, the Pose-C-Net, and the Obj-C-Net models extract features from Fully-connect 3 layer, and OverFeat model extracts features from Fully-connect 8 layer. Their feature dimensions are 512 and 4,096 respectively, and these features were used to construct manifolds.

In the manifold construction by PCA, the eigenspace dimension of each object was decided based on cumulative contribution over 80%. The average dimension of each eigenspace was around 10 for all objects. The pixel feature dimension was 16,384.

All the features used are summarized as follows:

- **Pixel**: Raw pixel values
- **PCA**: Coefficients obtained from the pixel feature calculated by PCA
- **Obj-C-Net**: Deep learning-based feature trained with object category information including COIL-20
- **OverFeat**: Deep learning-based feature trained with object category information including ImageNet 2012 training set
- **Pose-R-Net** (Proposed): Deep learning-based feature trained with pose information represented directly by angle (deg.)
- **Pose-CyclicR-Net** (Proposed): Deep learning-based feature trained with pose information rep-
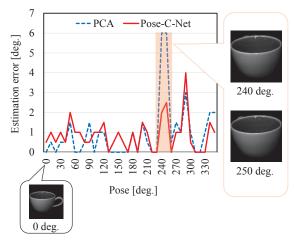
resented by trigonometric functions
- **Pose-C-Net** (Proposed): Deep learning-based feature trained with pose information represented as a categorical variable

## 4.3 Results and Discussion

Table 2 shows the experimental results. As for the evaluation criteria, we used Mean Absolute Error (MAE). The manifold constructed from features obtained from Pose-C-Net performed the best out of the eight manifolds. Features extracted from DCNNs trained with object category information; Obj-C-Net and OverFeat, showed low performance. We consider the reason for this is that they were trained without considering pose information. Features extracted from Pose-R-Net and Pose-CyclicR-Net showed lower performances than features extracted from Pose-C-Net. We consider the reason for this is that it is difficult for regression models to get rid of the effect of pose cyclicity. In contrast, Pose-C-Net manifold showed high accuracy because the classification model was not affected by pose cyclicity.

Next, we compared with the output of DCNNs shown in Table 3. All of the manifold-based pose estimation methods showed higher performances than all of the DCNN only methods. We considered the reason for this is that manifold-based pose estimation can estimate an unknown pose thanks to the interpolation.

Lastly, we investigate the effectiveness of the proposed method for an object which has very similar appearance poses. Figure 12 shows the experimental results. The object appearances are very similar between 240 deg. to 260 deg. since the handle of the cup is almost missing. It is difficult to estimate such poses exactly by features obtained by PCA because

of the small appearance change. In contrast, features extracted from Pose-C-Net shows better results than features obtained by PCA in such poses. We consider the reason for this is that Pose-C-Net was trained considering pose information, so features extracted from it can handle a pose change with slight appearance change without deteriorating the pose estimation accuracy of the other pose changes.

From the above results, we confirmed the effectiveness of the proposed method.

# 5 CONCLUSION

In this paper, we proposed an accurate pose estimation method named "Deep Manifold Embedding" which is a supervised feature extraction method for pose manifold using deep learning technique. We obtained pose discriminative features from deep learning trained with pose information. Manifolds constructed from the features were effective for pose estimation, especially in case of a pose change with a slight appearance change. Experimental results showed that the proposed method is effective compared with the conventional method which constructs manifolds from the features obtained by PCA. Here we conducted pose estimation experiments only around a specific rotation axis, but this method can estimate poses around an arbitrary rotation axises if there are corresponding training data.

As future work, we will consider a more suitable DCNN architecture, investigate the robustness to complex background and various illumination conditions, and compare with other state-of-the-art methods.

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